Fully Implicit Hurricane Modeling Jon Reisner, Andrzej Wyszogrodzki, Vincent Mousseau, and Dana Knoll

What's new about the model:

- A physics-based preconditioner has been developed that enables the large 3-D system to be computed in a reasonable amount of time
- 2) Higher-order in time solution procedures have been utilized (e.g., semi-implicit Runge-Kutta)
- Implicit AMR is being implemented into the model



Motivation

Over the last 25+ yr there has been little, if any, progress at improving the accuracy of hurricane intensity forecasts (e.g., Elsberry 1997; Emanuel 1998; Marks and Shay).

■AS ALWAYS WITH INTENSITY FORECASTS...I AM FULLY PREPARED TO BE WRONG IN EITHER DIRECTION.

FORECASTER LAWRENCE

FORECAST POSITIONS AND MAX WINDS

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INITIAL
           30/0300Z 19.2N 78.5W
                                  55 KTS
           30/1200Z 19.9N 79.6W
12HR VT
                                  60 KTS
          01/0000Z 21.2N 81.6W
24HR VT
                                  65 KTS
36HR VT
       01/1200Z 22.4N 84.0W
                                  70 KTS
       02/0000Z 23.9N 86.3W
                                  80 KTS
48HR VT
           03/0000Z 27.0N 90.0W
                                  90 KTS
72HR VT
```

46A 26.60 -90.30 10/03/00Z 125 940 HURRICANE-4



Model Equation Set + Solution Proceedure

- ■The chosen equation set is Navier-Stokes plus additional equations to represent precipitation processes (e.g., condensation and falling).
- ■The equation set is solved via the Jacobian Free Newton-Krylov approach.
- A time-split algorithm capable of solving the Navier-Stokes equation set is used to precondition the fully implicit equation set.
- A parabolic equation is solved in the preconditioner.

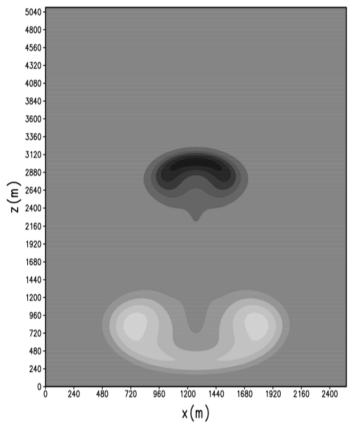


Accuracy and Efficiency of the Model

- ■A 2-D form of the hurricane equation set has been used to determine the accuracy and efficiency of the target equation set.
- ■The 2-D equation set has been used in the simulation of moist and dry thermals (Reisner et al., 2003, JCP).



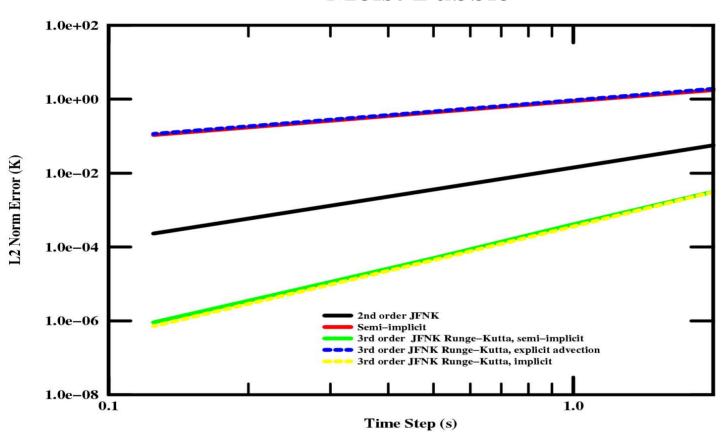
2-D Moist Precipitating Bubble



GrADS: COLA/UMCP



L2 Norm Versus Time Step Size For Moist Bubble





Navier-Stokes without Forcing (Con't)

Physics-Based Preconditioner reduces Krylov Iterations and Timings by a Factor of 10

Type	# of SSOR Cycles	Newt./dt	GMRES/ Newt.	Time(s)	Size
Precon=0		1.97	160.	4550.	64x64
Precon=0		1.98	170.	46283. (10.17)	128x128
Multigrid	2	1.93	15.83	475.	64x64
Multigrid	2	1.98	16.00	4756. (10.01)	128x128
Multigrid	2	2.00	15.45	52526. (11.04)	256x256

Note, this is for a 2nd order method, for a 3rd order method the factor is at least a factor of 100



Do the results from the 2-D Simulations Hold for the Hurricane?

Do time-split algorithms need to run at a time step that resolves that fastest wave in order to produce an accurate hurricane intensity forecast?

Will the physics-based preconditioner be able to reduce the number of Krylov iterations such that the algorithm is able to run efficiently in 3-D?



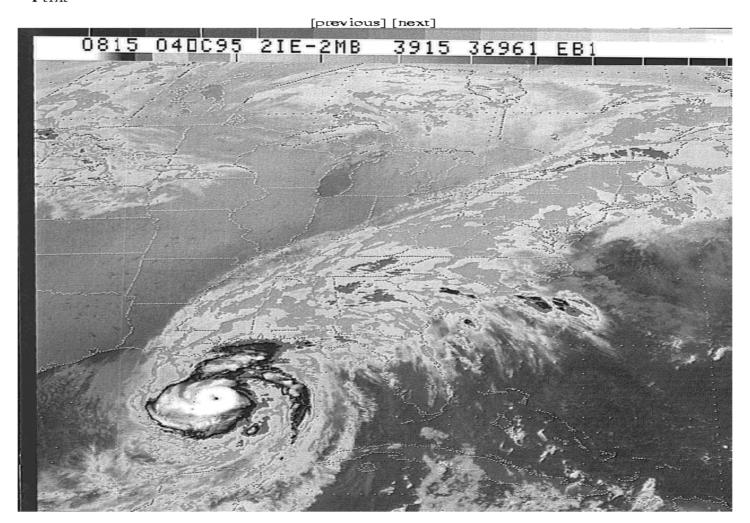


Fig. 11. Infrared (IR) GOES-8 satellite image for 0815 UTC 4 Oct 1995, operational MB curve enhancement.



Track of Hurricane Opal and Location of Warm-Core Eddy (WCE)



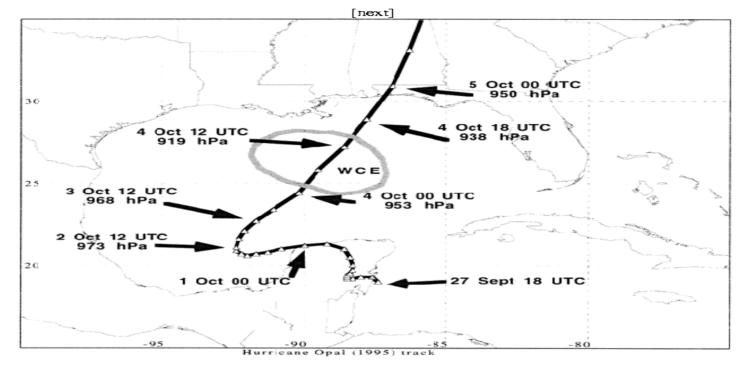


Fig. 1. Track of Hurricane Opal over the period 27 Sep-5 Oct 1995. Storm position indicated every 6 h by the open triangles. Storm central pressure (hPa) is indicated at selected time periods. Warm-core eddy (WCE) outlined in gray.

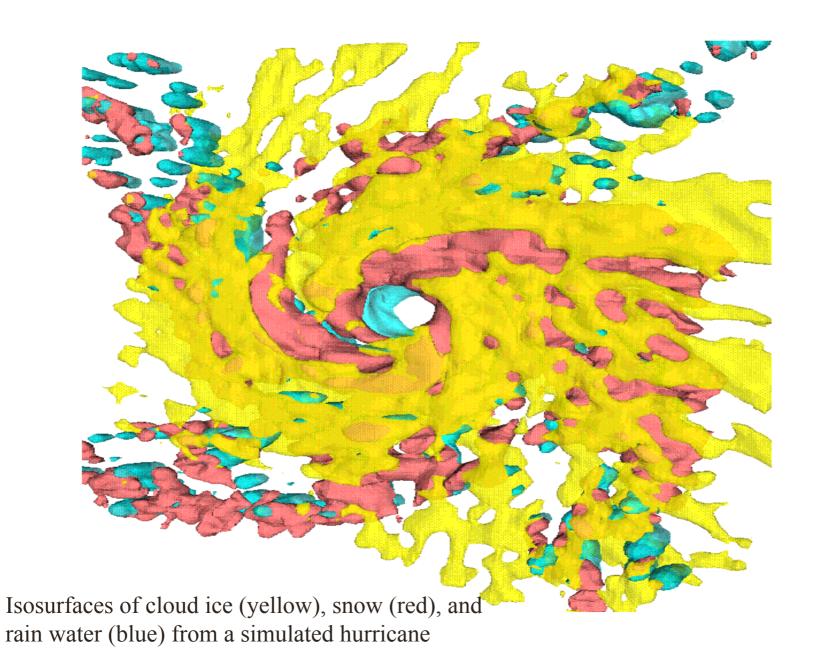
Bosart et al. 2000, MWR, 128, 322-252



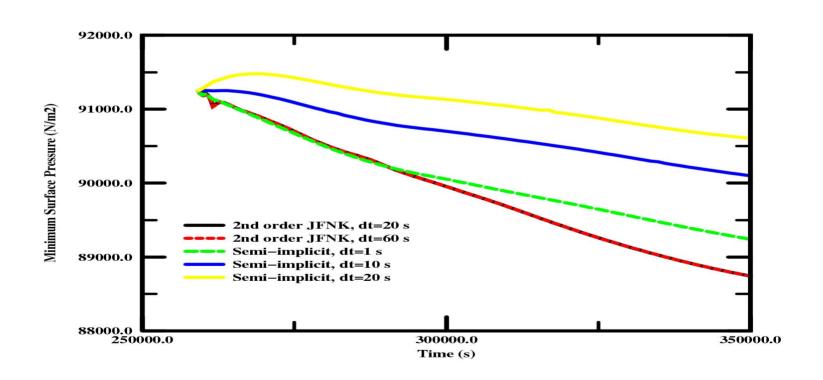
Hurricane Model Settup

- Idealized hurricane simulations employing 150x150x51 grid points with 10 km horizontal resolution and 300 m vertical resolution have been run.
- An idealized hurricane simulation was run until an approximate steady-state solution was reached. This involved about 3.0 days of actual time and about 2 days of computer time on 25 alpha processors.
- Next various idealized hurricane simulations utilizing different numerical approaches and time step sizes were run for a warmer sea-surface temperature using the above steady-state solution as an initial guess.



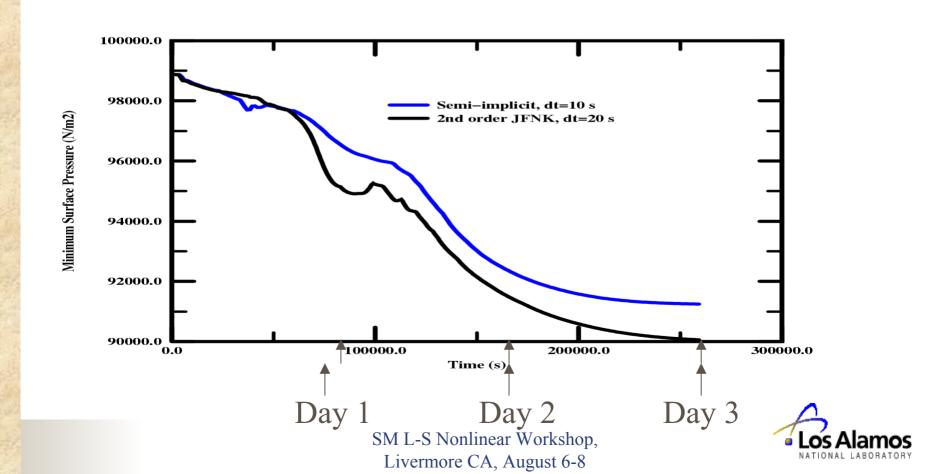


Hurricane Results (con't) Minimum Surface Pressure Versus Time From JFNK or Split Solvers





Minimum Surface Pressure Versus Time



Efficiency of Preconditioner Used in Hurricane Simulations

Δt	GMRES- PRE	Time-Pre	GMRES- NoPre	Time- NoPre
5	13	41	43	89
10	14	42	72	125
20	14	43	102	155
40	17	44	378	590
60	22	46	519	780
90	60	63	728	1400
120	75	85	910	

SM L-S Nonlinear Workshop, Livermore CA, August 6-8

Los Alamos

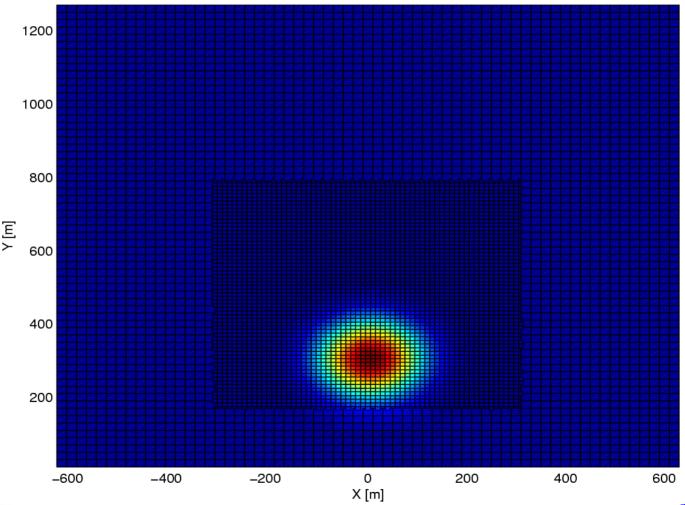
Implicit AMR: We need any helpful suggestions?

- Over the past year have "rewritten" a parallel AMR solver developed at NASA, PARAMESH, to allow for implicit AMR
- Target problem is currently a dry 2-D bubble incorporating a relatively complex two TKE level turbulence model
- Able to achieve higher-order accuracy in time for a static mesh, moving mesh is more difficult...



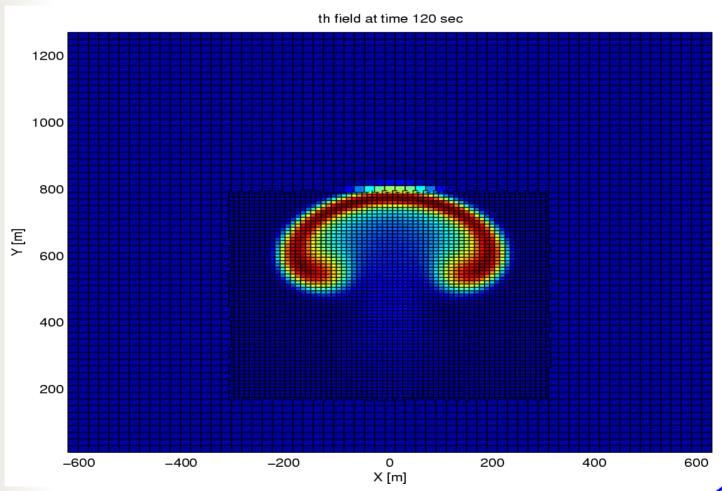
Static Mesh, Potential Temperature

th field at time 10 sec





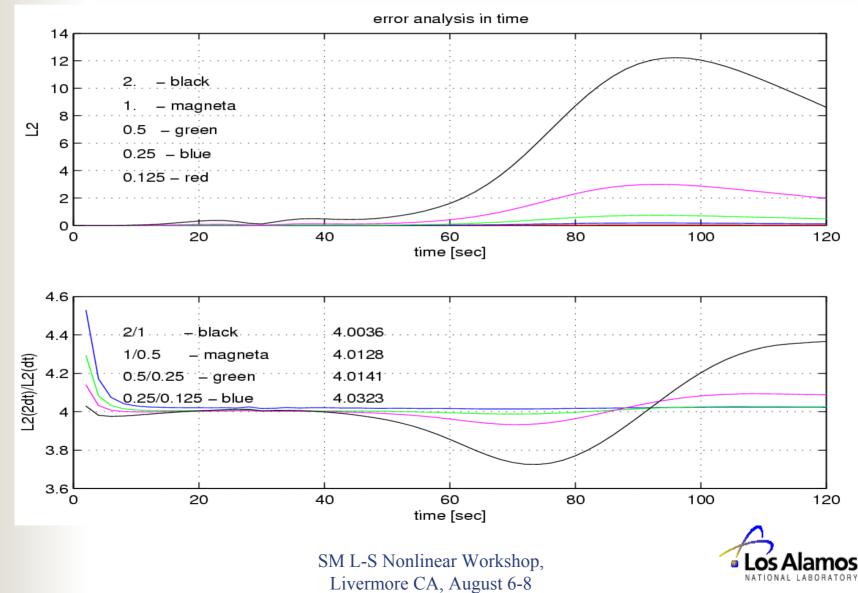
Static Mesh, Potential Temperature

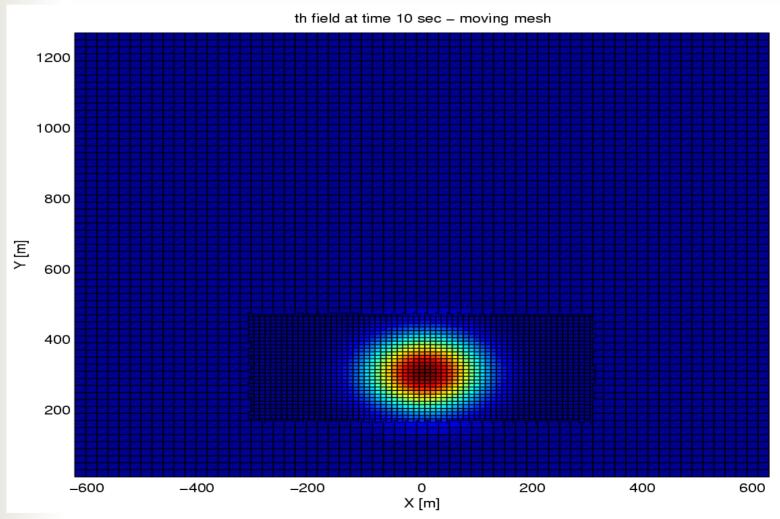




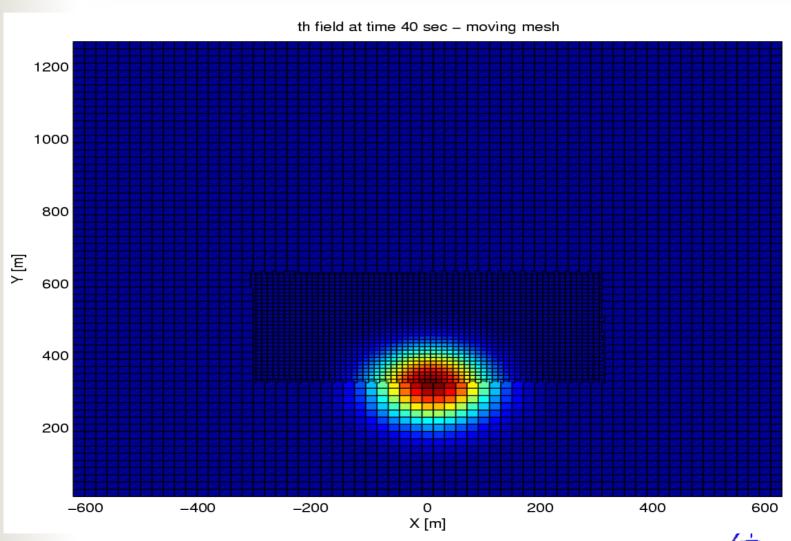


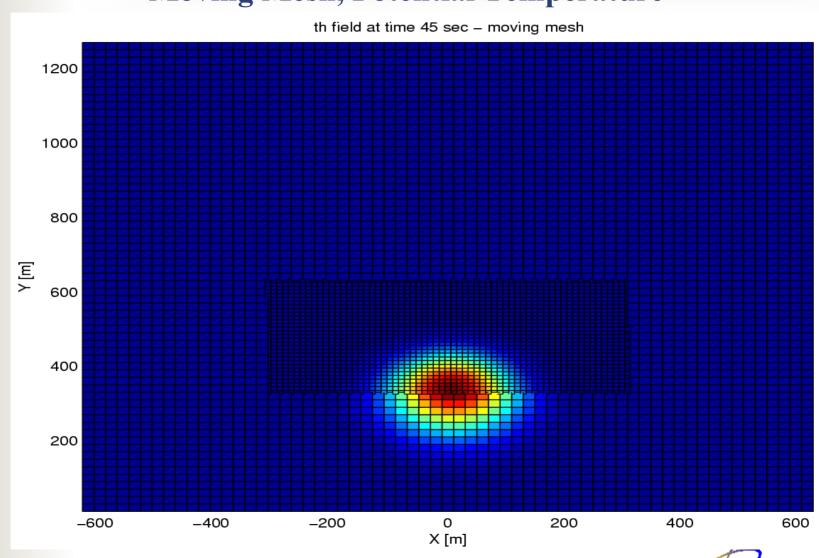
Static Mesh, Error Analysis

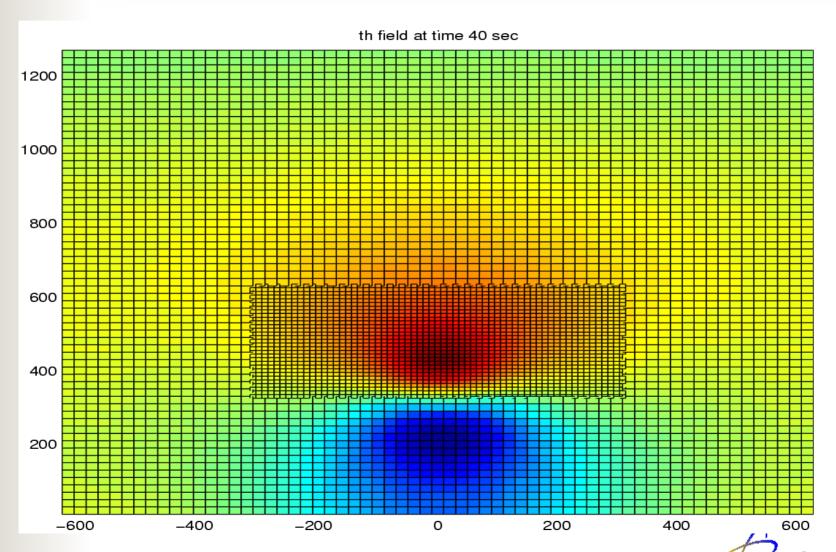


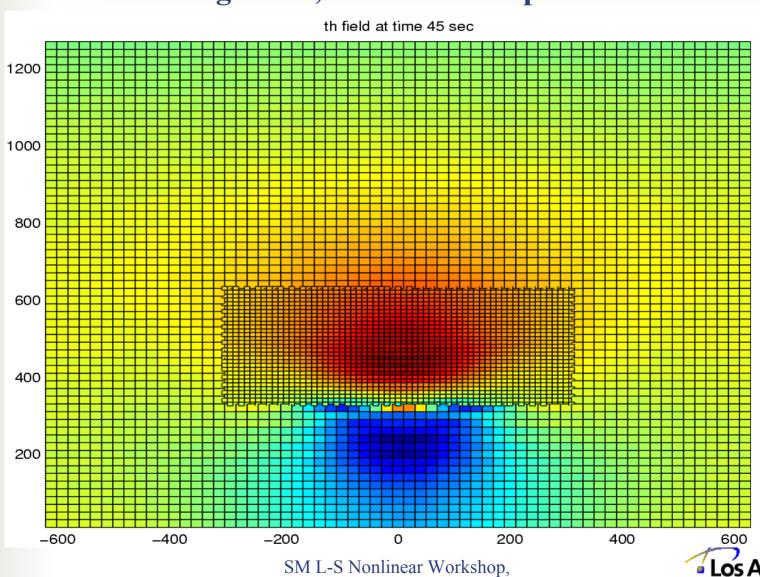






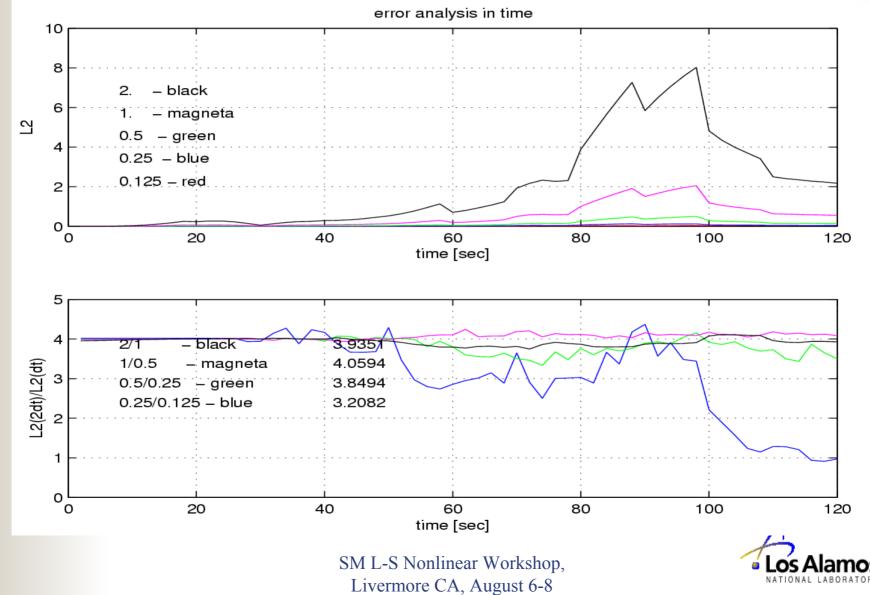






Livermore CA, August 6-8

Moving Mesh, Error Analysis



Future Plans

- ■Extend AMR solver into 3-D. Target applications are as follows:
 - A global code of Mars linked to a sub-surface model (Where's the water?)
 - Wildfires
- ■Continue to study higher-order time differencing formulations

